

Package ‘CompRandFld’

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Title Composite-likelihood based Analysis of Random Fields

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Description The aim of this package is to collect a set of procedures for the analysis of Random Fields by Composite Likelihood methods. Spatial analysis often involves dealing with large dataset. Therefore even simple studies may be too computationally demanding. Composite likelihood based methods are emerging as useful tools for mitigating such computational problems and show satisfactory results when compared with other techniques such as, for example the tapering method. Moreover, composite likelihood (and related quantities) have some good properties similar to those of the standard likelihood.

Suggests RandomFields, spam, scatterplot3d

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CheckCorrModel	<i>Checking Correlation Model</i>
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Description

Subroutine called by InitParam. The procedure controls if the correlation model inserted is correct.

Usage

```
CheckCorrModel(corrmodel)
```

Arguments

corrmodel String; the name of a correlation model, for the description see [CovarianceFct](#).

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See Also[FitComposite](#)

`CheckInput`*Checking Input*

Description

Subroutine called by the fitting procedures. The procedure controls the the validity of the input inserted by the users.

Usage

```
CheckInput(coordx, coordy, coordt, corrmodel, data, fcall, fixed, grid,
           likelihood, lonlat, margins, maxdist, maxtime, model, numblock,
           optimizer, param, replicates, start, taper, threshold, type,
           varest, vartype, weighted)
```

Arguments

<code>coordx</code>	A numeric ($d \times 2$)-matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
<code>coordy</code>	A numeric vector assigning 1-dimension of coordinates; <code>coordy</code> is interpreted only if <code>coordx</code> is a numeric vector otherwise it will be ignored.
<code>coordt</code>	A numeric vector assigning 1-dimension of temporal coordinates.
<code>corrmodel</code>	String; the name of a correlation model, for the description see FitComposite .
<code>data</code>	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
<code>fcall</code>	String; <code>Fitting</code> to call the fitting procedure and <code>simulation</code> to call the simulation.
<code>fixed</code>	A named list giving the values of the parameters that will be considered as known values. The listed parameters for a given correlation function will be not estimated, i.e. if <code>list(nugget=0)</code> the nugget effect is ignored.
<code>grid</code>	Logical; if <code>FALSE</code> (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if <code>TRUE</code> then $(d \times d \times n)$ -matrix is considered.
<code>likelihood</code>	String; the configuration of the composite likelihood. <code>Marginal</code> is the default.
<code>lonlat</code>	Logical; if <code>FALSE</code> (the default), <code>coordx</code> and <code>coordy</code> are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
<code>margins</code>	String; the type of the marginal distribution of the max-stable field.
<code>maxdist</code>	Numeric; an optional positive value indicating the maximum spatial distance considered in the composite-likelihood computation.
<code>maxtime</code>	Numeric; an optional positive value indicating the maximum temporal lag separation in the composite-likelihood.
<code>model</code>	String; the density associated to the likelihood objects. <code>Gaussian</code> is the default.

numblock	Numeric; the number of observation of the underlying random field (only for max-stable simulations). See RFSim .
optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.
param	A numeric vector of parameters, needed only in simulation. See RFSim .
replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.
start	A named list with the initial values of the parameters that are used by the numerical routines in maximization procedure. NULL is the default.
taper	String; the name of the tapered correlation function.
threshold	Numeric; a value indicating a threshold for the binary random field.
type	String; the type of the likelihood objects. If <code>Pairwise</code> (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.
varest	Logical; if TRUE the estimate' variances and standard errors are returned. FALSE is the default.
vartype	String; the type of estimation method for computing the estimate variances, see FitComposite .
weighted	Logical; if TRUE the likelihood objects are weighted. If FALSE (the default) the composite likelihood is not weighted.

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See Also

[FitComposite](#)

CheckLikelihood

Checking Composite-likelihood Type

Description

Subroutine called by `InitParam`. The procedure controls the type of the composite-likelihood inserted by the users.

Usage

```
CheckLikelihood(likelihood)
```

Arguments

`likelihood` String; the configuration of the composite likelihood. `Marginal` is the default.

Author(s)

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See Also

[FitComposite](#)

CheckModel

Checking Random Field type

Description

Subroutine called by InitParam. The procedure controls the type of random field inserted by the users.

Usage

CheckModel(model)

Arguments

model String; the density associated to the likelihood objects. Gaussian is the default.

Author(s)

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See Also

[FitComposite](#)

CheckType

Checking Likelihood Objects

Description

Subroutine called by InitParam. The procedure controls the type of likelihood objects inserted by the users.

Usage

CheckType(type)

Arguments

type String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.

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See Also

[FitComposite](#)

CheckVarType

Checking Variance Estimates Type

Description

Subroutine called by InitParam. The procedure controls the method used to compute the estimates' variances.

Usage

CheckVarType(type)

Arguments

type String; the method used to compute the estimates' variances. If SubSamp (the default) the estimates' variances are computed by the sub-sampling method, see [FitComposite](#).

Author(s)

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See Also

[FitComposite](#)

CompLikelihood	<i>Optimizes the Composite log-likelihood</i>
----------------	---

Description

Subroutine called by FitComposite. The procedure estimates the model parameters by maximisation of the composite log-likelihood.

Usage

```
CompLikelihood(coordx, coordy, corrmodel, data, flagcorr,
               flagnuis, fixed, grid, likelihood, lonlat,
               lower, model, namescorr, namesnuis, namesparam,
               numparam, numparamcorr, optimizer, param,
               spacetime, threshold, type, upper, varest,
               vartype, winconst, winstp)
```

Arguments

coordx	A numeric ($d \times 2$)-matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
corrmodel	Numeric; the id of the correlation model.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
flagcorr	A numeric vector of binary values denoting which parameters of the correlation function will be estimated.
flagnuis	A numeric vector of binary values denoting which nuisance parameters will be estimated.
fixed	A numeric vector of parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the compositelikelihood, see FitComposite .
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
lower	A numeric vector with the lower bounds of the parameters' ranges.
model	Numeric; the id value of the density associated to the likelihood objects.
namescorr	String; the names of the correlation parameters.
namesnuis	String; the names of the nuisance parameters.
namesparam	String; the names of the parameters to be maximised.
numparam	Numeric; the number of parameters to be maximised.
numparamcorr	Numeric; the number of correlation parameters.

optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.
param	A numeric vector of parameters' values.
spacetime	Logical; if TRUE the random field is spatial-temporal otherwise is a spatial field.
threshold	Numeric; a value indicating a threshold for the binary random field, see FitComposite .
type	String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.
upper	A numeric vector with the upper bounds of the parameters' ranges.
varest	Logical; if TRUE the estimate' variances and standard errors are returned. FALSE is the default.
vartype	String; the type of estimation method for computing the estimate variances, see FitComposite .
winconst	Numeric; a positive value – if vartype=SubSamp – determines the window size in the sub-sampling estimates of the variances, see FitComposite .
winstp	Numeric; a positive value – if vartype=SubSamp – determines the window step in the sub-sampling estimates of the variances, see FitComposite .

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See Also

[FitComposite](#)

CorrelationParam *Lists the Parameters of a Correlation Model*

Description

Subroutine called by InitParam and other procedures. The procedure returns a list with the parameters of a given correlation model.

Usage

```
CorrelationParam(corrmodel)
```

Arguments

corrmodel String; the name of a correlation model.

Author(s)

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See Also[FitComposite](#)

Covariogram

*Computes covariance, variogram and extremal coefficient functions***Description**

The procedure computes and/or plots the covariance, the variogram or the extremal coefficient functions and the practical range estimated fitting a Gaussian or max-stable random field with the composite-likelihood or using the weighted least square method. Allows to add to the variogram or extremal coefficient plots the empirical estimates.

Usage

```
Covariogram(fitted, lags=NULL, lagt=NULL, answer.cov=FALSE, answer.vario=FALSE,
            answer.extc=FALSE, answer.range=FALSE, fix.lags=NULL, fix.lagt=NULL,
            show.cov=FALSE, show.vario=FALSE, show.extc=FALSE, show.range=FALSE,
            add.cov=FALSE, add.vario=FALSE, add.extc=FALSE, pract.range=95,
            vario, ...)
```

Arguments

<code>fitted</code>	A fitted object obtained from the FitComposite or WLeastSquare procedures.
<code>lags</code>	A numeric vector of distances.
<code>lagt</code>	A numeric vector of temporal separations.
<code>answer.cov</code>	Logical; if TRUE a vector with the estimated covariance function is returned; if FALSE (the default) the covariance is not returned.
<code>answer.vario</code>	Logical; if TRUE a vector with the estimated variogram is returned; if FALSE (the default) the variogram is not returned.
<code>answer.extc</code>	Logical; if TRUE a vector with the estimated extremal coefficient is returned; if FALSE (the default) the variogram is not returned.
<code>answer.range</code>	Logical; if TRUE the estimated practical range is returned; if FALSE (the default) the practical range is not returned.
<code>fix.lags</code>	Integer; a positive value denoting the spatial lag to consider for the plot of the temporal profile.
<code>fix.lagt</code>	Integer; a positive value denoting the temporal lag to consider for the plot of the spatial profile.
<code>show.cov</code>	Logical; if TRUE the estimated covariance function is plotted; if FALSE (the default) the covariance function is not plotted.
<code>show.vario</code>	Logical; if TRUE the estimated variogram is plotted; if FALSE (the default) the variogram is not plotted.
<code>show.extc</code>	Logical; if TRUE the estimated extremal coefficient is plotted; if FALSE (the default) the extremal coefficient is not plotted.

<code>show.range</code>	Logical; if TRUE the estimated practical range is added on the plot; if FALSE (the default) the practical range is not added.
<code>add.cov</code>	Logical; if TRUE the vector of the estimated covariance function is added on the current plot; if FALSE (the default) the covariance is not added.
<code>add.vario</code>	Logical; if TRUE the vector with the estimated variogram is added on the current plot; if FALSE (the default) the correlation is not added.
<code>add.extc</code>	Logical; if TRUE the vector with the estimated extremal coefficient is added on the current plot; if FALSE (the default) the correlation is not added.
<code>pract.range</code>	Numeric; the percent of the sill to be reached.
<code>vario</code>	A Variogram object obtained from the EVariogram procedure.
<code>...</code>	other optional parameters which are passed to plot functions.

Value

The returned object is eventually a list with:

<code>covariance</code>	The vector of the estimated covariance function;
<code>variogram</code>	The vector of the estimated variogram function;
<code>extrcoeff</code>	The vector of the estimated extremal coefficient function;
<code>practical.range</code>	The estimated practical range.

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References

Gaetan, C. and Guyon, X. (2010) Spatial Statistics and Modelling. *Spring Verlag, New York.*

See Also

[FitComposite](#), [WLeastSquare](#)

Examples

```
library(CompRandFld)
library(RandomFields)
library(scatterplot3d)
set.seed(31231)

# Set the coordinates of the points:
x <- runif(100, 0, 10)
y <- runif(100, 0, 10)

#####
###
```

```

### Example 1. Plot of covariance and variogram functions
### estimated from a Gaussian random field with exponent
### correlation. One spatial replication is simulated.
###
###
#####

# Set the model's parameters:
corrmodel <- "exponential"
mean <- 0
sill <- 1
nugget <- 0
scale <- 3

# Simulation of the Gaussian random field:
data <- RFsim(x, y, corrmodel=corrmodel, param=list(mean=mean,
            sill=sill, nugget=nugget, scale=scale))$data

# Maximum composite-likelihood fitting of the Gaussian random field:
fit <- FitComposite(data, x, y, corrmodel=corrmodel,
            type='Difference')

# Empirical estimation of the variogram:
vario <- EVariogram(data, x, y)

# Plot of covariance and variogram functions:
par(mfrow=c(1,2))
Covariogram(fit, show.cov=TRUE, show.range=TRUE,
            show.vario=TRUE, vario=vario)

#####
##
### Example 2. Plot of covariance and extremal coefficient
### functions estimated from a max-stable random field with
### exponential correlation. n idd spatial replications are
### simulated.
###
#####

set.seed(1126)
# Simulation of the max-stable random field:
data <- RFsim(x, y, corrmodel=corrmodel, model="ExtGauss", replicates=20,
            param=list(mean=mean,sill=sill,nugget=nugget,scale=scale))$data

# Maximum composite-likelihood fitting of the max-stable random field:
fit <- FitComposite(data, x, y, corrmodel=corrmodel, model='ExtGauss',
            replicates=20, varest=TRUE, vartype='Sampling',
            margins="Frechet")

data <- Dist2Dist(data, to='sGumbel')

# Empirical estimation of the madogram:

```

```

vario <- EVariogram(data, x, y, type='madogram', replicates=20)

# Plot of correlation and extremal coefficient functions:
par(mfrow=c(1,2))
Covariogram(fit, show.cov=TRUE, show.range=TRUE, show.extc=TRUE,
            vario=vario, pract.range=84)

#####
###
### Example 3. Plot of covariance and variogram functions
### estimated from a Gaussian spatio-temporal random field with
### double-exp correlation.
### One spatio-temporal replication is simulated.
###
#####

# Define the spatial-coordinates of the points:
x <- runif(20, 0, 1)
y <- runif(20, 0, 1)
# Define the temporal sequence:
time <- seq(0, 50, 1)

# Simulation of the spatio-temporal Gaussian random field:
data <- RFsim(x, y, time, corrmodel="exp_exp",param=list(mean=mean,
              nugget=nugget,scale_s=0.5,scale_t=1,sill=sill))$data

# Maximum composite-likelihood fitting of the space-time Gaussian random field:
fit <- FitComposite(data, x, y, time, corrmodel="exp_exp", maxtime=5,
                  likelihood="Marginal",type="Pairwise", fixed=list(
                    nugget=nugget, mean=mean),start=list(scale_s=0.2,
                    scale_t=1, sill=sill))

# Empirical estimation of spatio-temporal covariance:
vario <- EVariogram(data, x, y, time, maxtime=10)

# Plot of the fitted space-time covariace
Covariogram(fit,show.cov=TRUE)

# Plot of the fitted space-time variogram
Covariogram(fit,vario=vario,show.vario=TRUE)

# Plot of covariance, variogram and spatio and temporal profiles:
Covariogram(fit,vario=vario,fix.lagt=1,fix.lags=1,show.vario=TRUE)

#####
###
### Example 4. Plot of parametric and empirical lorelograms
### estimated from a Binary Gaussian random fields with
### exponential correlation. One spatial replication is
### simulated.
###
#####

```

```

set.seed(1240)

# Define the spatial-coordinates of the points:
x <- seq(0,3, 0.1)
y <- seq(0,3, 0.1)

# Simulation of the Binary Gaussian random field:
data <- RFsim(x, y, corrmodel=corrmodel, model="BinaryGauss",
             threshold=0,param=list(nugget=nugget,mean=mean,
                                   scale=.6,sill=0.8))$data

# Maximum composite-likelihood fitting of the Binary Gaussian random field:
fit <- FitComposite(data, x, y, corrmodel=corrmodel, model="BinaryGauss",
                  maxdist=0.8, likelihood="Marginal", type="Pairwise",
                  start=list(mean=mean,scale=0.1,sill=0.1))

# Empirical estimation of the lorelogram:
vario <- EVariogram(data, x, y, type="lorelogram", maxdist=2)

# Plot of fitted and empirical lorelograms:
Covariogram(fit, vario=vario, show.vario=TRUE, lags=seq(0.1,2,0.1))

```

Dist2Dist

Switches from an EV to Another EV Distribution

Description

The function transforms observations belonging to the GEV class from one model to another.

Usage

```
Dist2Dist(data, from='Gev', to='sFrechet', loc=NULL, scale=NULL, shape=NULL)
```

Arguments

data	A numeric vector or a matrix of extreme values.
from	The name of the original extreme value distribution, i.e. Gev (the default), see the Details section.
to	The name of the desired extreme value distribution, i.e. sFrechet (the default), see the Details section.
loc	A numeric value or vector of location parameters.
scale	A numeric value or vector of scale parameters.
shape	A numeric value or vector of shape parameters.

Details

If data is a numeric vector of length n then the dataset is considered as a realisation from an univariate extreme value distribution. Instead, if data is a $(n \times d)$ -matrix then the columns represent the different variables with extreme value distributions and the rows represent the iid replications. Finally, if data is a $(d \times d \times n)$ -matrix then the columns and rows represent the different variables and the third dimension represents the iid replications.

The parameters `from` and `to` indicate the original extreme value distribution(s) from which the observations are drawn and the target extreme value distribution(s) that the transformed data will follow. The options are:

1. `from=Gev` (generalised extreme value distribution):
 - `to=Uniform`, which means uniform distribution;
 - `to=sFrechet`, which means standard (or unit) Frechet distribution, that is $GEV(1,1,1)$;
 - `to=sGumbel`, which means standard Gumbel distribution, that is $GEV(0,1,1)$;
 - `to=sWeibull`, which means standard Weibull distribution, that is $GEV(1,1,-1)$;
 - `to=Gev`, which means generalised extreme value distribution. Note, that in this case, it is required to insert vectors of location, scale and shape parameters with dimension n in the univariate case, dimension d when data is $(n \times d)$ -matrix and dimension $n \times d$ when data is $(d \times d \times n)$ -matrix.
2. `from=sFrechet`
 - `to=Gev`.
3. `from=sGumbel`
 - `to=Gev`.
4. `from=sWeibull`
 - `to=Gev`.

Value

A numeric vector or matrix of transformed values following the desired distribution.

Author(s)

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References

de Haan, L. and Ferreira, A. (2006) *Extreme Value Theory An Introduction*. Springer Verlag, New York.

See Also

[FitGev](#)

EVariogram	<i>Empirical Variogram(variants) of Gaussian, Binary and Max-Stable Fields</i>
------------	--

Description

The function returns an empirical estimate of the variogram (or its variants) for Gaussian, Binary and max-stable random field.

Usage

```
EVariogram(data, coordx, coordy, coordt=NULL, cloud=FALSE, grid=FALSE,
            gev=c(0,1,0), lonlat=FALSE, maxdist=NULL, maxtime=NULL,
            numbins=NULL, replicates=1, type='variogram')
```

Arguments

data	A d -dimensional vector (a single spatial realisation) or a $(n \times d)$ -matrix (n iid spatial realisations) or a $(d \times d)$ -matrix (a single spatial realisation on regular grid) or an $(d \times d \times n)$ -array (n iid spatial realisations on regular grid) or a $(t \times d)$ -matrix (a single spatial-temporal realisation) or an $(t \times d \times n)$ -array (n iid spatial-temporal realisations) or or an $(d \times d \times t \times n)$ -array (a single spatial-temporal realisation on regular grid) or an $(d \times d \times t \times n)$ -array (n iid spatial-temporal realisations on regular grid). See FitComposite for details.
coordx	A numeric $(d \times 2)$ -matrix (where d is the number of spatial sites) assigning 2-dimensions of spatial coordinates or a numeric d -dimensional vector assigning 1-dimension of spatial coordinates.
coordy	A numeric vector assigning 1-dimension of spatial coordinates; coordy is interpreted only if coordx is a numeric vector or grid=TRUE otherwise it will be ignored. Optional argument, the default is NULL then coordx is expected to be numeric a $(d \times 2)$ -matrix.
coordt	A numeric vector assigning 1-dimension of temporal coordinates. Optional argument, the default is NULL then a spatial random field is expected.
cloud	Logical; if TRUE the variogram cloud is computed, otherwise if FALSE (the default) the empirical (binned) variogram is returned.
grid	Logical; if FALSE (the default) the data are interpreted as spatial or spatial-temporal realisations on a set of non-equispaced spatial sites.
gev	A numeric vector with the three GEV parameters;
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
maxdist	A numeric value denoting the spatial maximum distance, see the Section Details .
maxtime	A numeric value denoting the temporal maximum distance, see the Section Details .

numbins	A numeric value denoting the numbers of bins, see the Section Details .
replicates	Numeric; a positive integer denoting the number of independent and identically distributed (iid) replications of a spatial or spatial-temporal random field. Optional argument, the default value is 1 then a single realisation is considered.
type	A String denoting the type of variogram. Four options are available: <code>variogram</code> , <code>madogram</code> , <code>Fmadogram</code> and <code>lorelogram</code> . It is returned respectively, the standard variogram with the first (Gaussian responses), the madogram with the second and third (extreme values), the lorelogram with the fourth (Binary data).

Details

We briefly report the definitions of variogram used in this function.

In the case of a spatial Gaussian random field the sample `variogram` estimator is defined by

$$\hat{\gamma}(h) = 0.5 \sum_{x_i, x_j \in N(h)} (Z(x_i) - Z(x_j))^2 / |N(h)|$$

where $N(h)$ is the set of all the sample pairs whose distances fall into a tolerance region with size h (equispaced intervals are considered). Observe, that in the literature often the above definition is termed semivariogram (see e.g. the first reference). Nevertheless, here this definition has been used in order to be consistent with the variogram definition used for the extremes (see e.g. the third reference).

In the case of a spatial max-stable random field, the sample `madogram` estimator is defined similarly to the Gaussian case by

$$\hat{\nu}(h) = 0.5 \sum_{x_i, x_j \in N(h)} |Z(x_i) - Z(x_j)| / |N(h)|.$$

In the case of a spatial binary random field, the sample `lorelogram` estimator (the analogue of the correlation) is defined by

$$\hat{L}(h) = (N_{11}(h)N_{00}(h)) / (N_{01}(h)N_{10}(h)).$$

where $N_{11}(h)$ is the number of pairs who are both equal to 1 and that falls in the bin h . Similarly are defined the other quantities.

In the case of a spatio-temporal Gaussian random field the sample `variogram` estimator is defined by

$$\hat{\gamma}(h, u) = 0.5 \sum_{(x_i, l), (x_j, k) \in N(h, u)} (Z(x_i, l) - Z(x_j, k))^2 / |N(h, u)|$$

where $N(h, u)$ is the set of all the sample pairs whose spatial distances fall into a tolerance region with size h and $|k - l| = u$. Note, that $Z(x_i, l)$ is the observation at site x_i and time l . Taking this in mind and given the above definition of lorelogram, the spatio-temporal extension is straightforward.

The `numbins` parameter indicates the number of adjacent intervals to consider in order to grouped distances with which to compute the (weighted) least squares.

The `maxdist` parameter indicates the maximum spatial distance below which the shorter distances will be considered in the calculation of the (weighted) least squares.

The `maxtime` parameter indicates the maximum temporal distance below which the shorter distances will be considered in the calculation of the (weighted) least squares.

Value

Returns an object of class `Variogram`. An object of class `Variogram` is a list containing at most the following components:

<code>bins</code>	Adjacent intervals of grouped spatial distances if <code>cloud=FALSE</code> . Otherwise if <code>cloud=TRUE</code> all the spatial pairwise distances;
<code>bint</code>	Adjacent intervals of grouped temporal distances if <code>cloud=FALSE</code> . Otherwise if <code>cloud=TRUE</code> all the temporal pairwise distances;
<code>cloud</code>	If the variogram cloud is returned (<code>TRUE</code>) or the empirical variogram (<code>FALSE</code>);
<code>centers</code>	The centers of the spatial bins;
<code>extcoeff</code>	The spatial extremal coefficient function. Available only if <code>type</code> is equal to <code>madogram</code> or <code>Fmadogram</code> (for the moment available only for a spatial random field);
<code>lenbins</code>	The number of pairs in each spatial bin;
<code>lenbinst</code>	The number of pairs in each spatial-temporal bin;
<code>lenbint</code>	The number of pairs in each temporal bin;
<code>srange</code>	The maximum and minimum spatial distances used for the calculation of the variogram;
<code>variograms</code>	The empirical spatial variogram;
<code>variogramst</code>	The empirical spatial-temporal variogram;
<code>variogramt</code>	The empirical temporal variogram;
<code>trange</code>	The maximum and minimum temporal distance used for the calculation of the variogram;
<code>type</code>	The type of estimated variogram: the standard variogram or the madogram.

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See Also

[FitComposite](#)

Examples

```

library(CompRandFld)
library(RandomFields)
set.seed(514)

# Set the coordinates of the sites:
x <- runif(200, 0, 10)
y <- runif(200, 0, 10)

#####
###
### Example 1. Empirical estimation of the variogram from a
### Gaussian random field with exponential correlation.
### One spatial replication is simulated.
###
###
#####

# Set the model's parameters:
corrmodel <- "exponential"
mean <- 0
sill <- 1
nugget <- 0
scale <- 3

# Simulation of the spatial Gaussian random field:
data <- RFsim(x, y, corrmodel=corrmodel, param=list(mean=mean,
            sill=sill, nugget=nugget, scale=scale))$data

# Empirical spatial variogram estimation:
fit <- EVariogram(data, x, y)

# Results:
plot(fit$centers, fit$variograms, xlab='h', ylab=expression(gamma(h)),
     ylim=c(0, max(fit$variograms)), xlim=c(0, fit$srange[2]), pch=20,
     main="variogram")

#####
###
### Example 2. Empirical estimation of the variogram from a
### spatio-temporal Gaussian random fields with Gneiting
### correlation function.
### One spatial replication is simulated
###
#####

set.seed(331)
# Define the temporal sequence:
times <- seq(1,15,1)

```

```

# Simulation of a spatio-temporal Gaussian random field:
data <- RFsim(x, y, times, corrmmodel="gneiting",
             param=list(mean=0,scale_s=3,scale_t=3,sill=sill,
                       nugget=0,power_s=1,power_t=1,sep=0.2))$data

# Empirical spatio-temporal variogram estimation:
fit <- EVariogram(data, x, y, times, maxtime=10)

# Results: Marginal spatial empirical variogram
par(mfrow=c(2,2), mai=c(.5,.5,.3,.3), mgp=c(1.4,.5, 0))
plot(fit$centers, fit$variograms, xlab='h', ylab=expression(gamma(h)),
     ylim=c(0, max(fit$variograms)), xlim=c(0, max(fit$centers)),
     pch=20,main="Marginal spatial Variogram",cex.axis=.8)

# Results: Marginal temporal empirical variogram
plot(fit$bint, fit$variogramt, xlab='t', ylab=expression(gamma(t)),
     ylim=c(0, max(fit$variograms)),xlim=c(0,max(fit$bint)),
     pch=20,main="Marginal temporal Variogram",cex.axis=.8)

# Building space-time variogram
st.vario <- matrix(fit$variogramst,length(fit$centers),length(fit$bint))
st.vario <- cbind(c(0,fit$variograms), rbind(fit$variogramt,st.vario))

# Results: 3d Spatio-temporal variogram
require(scatterplot3d)
st.grid <- expand.grid(c(0,fit$centers),c(0,fit$bint))
scatterplot3d(st.grid[,1], st.grid[,2], c(st.vario),
             highlight.3d=TRUE, xlab="h",ylab="t",
             zlab=expression(gamma(h,t)), pch=20,
             main="Space-time variogram",cex.axis=.7,
             mar=c(2,2,2,2), mgp=c(0,0,0),
             cex.lab=.7)

# A smoothed version
par(mai=c(.2,.2,.2,.2),mgp=c(1,.3, 0))
persp(c(0,fit$centers), c(0,fit$bint), st.vario,
      xlab="h", ylab="u", zlab=expression(gamma(h,u)),
      ltheta=90, shade=0.75, ticktype="detailed", phi=30,
      theta=30,main="Space-time variogram",cex.axis=.8,
      cex.lab=.8)

#####
###
### Example 3. Empirical estimation of the mandogram from a
### max-stable random field (Extremal Gaussian model) with
### exponential correlation.
### n iid spatial replications are simulated.
###
#####

set.seed(7273)
# Simulation of the max-stable random field:

```

```

data <- RFSim(x, y, corrmodel=corrmodel, model="ExtGauss",
             param=list(mean=mean, sill=sill, nugget=nugget,
                       scale=scale), replicates=40)$data
# Tranform data from from common unit Frechet to standard Gumbel margins:
data <- Dist2Dist(data, to='sGumbel')

# Empirical madogram estimation:
fit <- EVariogram(data, x, y, type='madogram', replicates=40, cloud=FALSE)

# Results:
par(mfrow=c(1,2), mai=c(.6,.6,.3,.3), mgp=c(1.6,.6, 0))
plot(fit$centers, fit$variograms, xlab='h', ylab=expression(nu(h)),
     ylim=c(0, max(fit$variograms)), xlim=c(0, fit$srange[2]), pch=20,
     main="madogram")
plot(fit$centers, fit$extcoeff, xlab='h', ylab=expression(theta(h)),
     ylim=c(1, 2), xlim=c(0, fit$srange[2]), pch=20,
     main="extremal coefficient")

#####
###
### Example 4. Empirical estimation of the lorelogram from a
### Binary-Gaussian random field with exponential correlation.
### One spatial replication is simulated.
###
###
#####

set.seed(1221)
# Simulation of the Binary-Gaussian random field:
data <- RFSim(x, y, corrmodel="exponential", model="BinaryGauss",
             param=list(mean=mean,sill=sill,scale=scale,nugget=nugget),
             threshold=0)$data

# Empirical lorelogram estimation:
fit <- EVariogram(data, x, y, numbins=20, maxdist=7, type="lorelogram")

# Results:
plot(fit$centers, fit$variograms, xlab='Distance', ylab="Lorelogram",
     ylim=c(min(fit$variograms), max(fit$variograms)),
     xlim=c(0, max(fit$centers)), pch=20, main="Spatial Lorelogram")

#####
###
### Example 5. Empirical estimation of the lorelogram from a
### spatio-temporal Binary-Gaussian random field with double
### exponential correlation.
### One spatial replication is simulated.
###
###
#####

set.seed(5351)
# Define the temporal sequence:

```

```

times <- seq(1,15,1)

# Simulation of othe space-time Binary Gaussian random field:

data <- RFsim(x, y, times, corrmmodel="exp_exp", model="BinaryGauss",
             threshold=0, param=list(nugget=nugget,mean=mean,scale_t=1.5,
             scale_s=1.5,sill=0.8))$data

# Empirical lorelogram estimation:
fit <- EVariogram(data, x, y, times, type="lorelogram", maxtime=8)

# Building space-time lorelogram
st.vario <- matrix(fit$variogramst,length(fit$centers),length(fit$bint))
tempvario <- rbind(fit$variogramt,st.vario)
st.vario <- cbind(c(NA,fit$variograms),tempvario)

par(mfrow=c(2,2))

# Results:
# Marginal spatial empirical lorelogram
plot(fit$centers, fit$variograms, xlab='h', ylab="lorelogram",
     xlim=c(0, max(fit$centers)), pch=20,main="Marginal spatial lorelgram")

# Marginal temporal empirical lorelogram
plot(fit$bint, fit$variogramt, xlab='t', ylab="lorelogram",
     xlim=c(0,max(fit$bint)), pch=20,main="Marginal temporal lorelogram")

# 3d Spatio-temporal lorelogram:
require(scatterplot3d)
st.grid <- expand.grid(c(0,fit$centers), c(0,fit$bint))

scatterplot3d(st.grid[,1], st.grid[,2], c(st.vario),
              highlight.3d=TRUE, xlab = "h", ylab = "t",
              zlab="Lorelogram",pch=20, main="Space-time lorelogram",
              cex.axis=.7, mar=c(2,2,2,2), mgp=c(0,0,0),cex.lab=.7)

# smoothed version:
par(mai=c(.2,.2,.2,.2),mgp=c(1.2,.5, 0))
persp(c(0,fit$centers),c(0,fit$bint),st.vario,
      xlab = "h", ylab = "t", zlab = "Lorelogram",
      ltheta=90, shade=0.75, ticktype="detailed",
      phi=30,theta=30, main="Space-time lorelogram",
      cex.axis=.8, cex.lab=.8)

```

Description

Maximum weighted composite-likelihood fitting of Gaussian, binary and max-stable random fields. The function returns the model parameters' estimates and the estimates' variances by weighted maximisation of the composite-likelihood and allows to fix any of the parameters.

Usage

```
FitComposite(data, coordx, coordy=NULL, coordt=NULL, corrmode1, fixed=NULL,
             grid=FALSE, likelihood='Marginal', lonlat=FALSE, margins='Gev',
             maxdist=NULL, maxtime=NULL, model='Gaussian', optimizer='Nelder-Mead',
             replicates=1, start=NULL, taper=NULL, threshold=NULL, type='Pairwise',
             varest=FALSE, vartype='SubSamp', weighted=FALSE, winconst, winstp)
```

Arguments

data	A d -dimensional vector (a single spatial realisation) or a $(n \times d)$ -matrix (n iid spatial realisations) or a $(d \times d)$ -matrix (a single spatial realisation on regular grid) or an $(d \times d \times n)$ -array (n iid spatial realisations on regular grid) or a $(t \times d)$ -matrix (a single spatial-temporal realisation) or an $(t \times d \times n)$ -array (n iid spatial-temporal realisations) or or an $(d \times d \times t \times n)$ -array (a single spatial-temporal realisation on regular grid) or an $(d \times d \times t \times n)$ -array (n iid spatial-temporal realisations on regular grid). For the description see the Section Details .
coordx	A numeric $(d \times 2)$ -matrix (where d is the number of spatial sites) assigning 2-dimensions of spatial coordinates or a numeric d -dimensional vector assigning 1-dimension of spatial coordinates.
coordy	A numeric vector assigning 1-dimension of spatial coordinates; coordy is interpreted only if coordx is a numeric vector or grid=TRUE otherwise it will be ignored. Optional argument, the default is NULL then coordx is expected to be numeric a $(d \times 2)$ -matrix.
coordt	A numeric vector assigning 1-dimension of temporal coordinates. At the moment implemented only for the Gaussian case. Optional argument, the default is NULL then a spatial random field is expected.
corrmode1	String; the name of a correlation model, for the description see the Section Details .
fixed	An optional named list giving the values of the parameters that will be considered as known values. The listed parameters for a given correlation function will be not estimated, i.e. if <code>list(nugget=0)</code> the nugget effect is ignored.
grid	Logical; if FALSE (the default) the data are interpreted as spatial or spatial-temporal realisations on a set of non-equispaced spatial sites (irregular grid).
likelihood	String; the configuration of the composite likelihood. Marginal is the default, see the Section Details .
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
margins	String; the type of the marginal distribution of the max-stable field. Gev is the default, see the Section Details .

maxdist	Numeric; an optional positive value indicating the maximum spatial distance considered in the composite-likelihood computation. See the Section Details for more information.
maxtime	Numeric; an optional positive value indicating the maximum temporal separation considered in the composite-likelihood computation (see Details).
model	String; the type of random field and therefore the densities associated to the likelihood objects. Gaussian is the default, see the Section Details .
optimizer	String; the optimization algorithm (see <code>optim</code> for details). 'Nelder-Mead' is the default.
replicates	Numeric; a positive integer denoting the number of independent and identically distributed (iid) replications of a spatial or spatial-temporal random field. Optional argument, the default value is 1 then a single realisation is considered.
start	An optional named list with the initial values of the parameters that are used by the numerical routines in maximization procedure. NULL is the default (see Details).
taper	String; the name of the taper correlation function, see the Section Details . Optional parameter considered only if the type parameter is equal to Tapering.
threshold	Numeric; a value indicating a threshold for the binary random field. Optional in the case that model is BinaryGauss, see the Section Details .
type	String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods (see Details).
varest	Logical; if TRUE the estimates' variances and standard errors are returned. FALSE is the default.
vartype	String; (SubSamp the default) the type of method used for computing the estimates' variances, see the Section Details .
weighted	Logical; if TRUE the likelihood objects are weighted, see the Section Details . If FALSE (the default) the composite likelihood is not weighted.
winconst	Numeric; a positive value for computing the sub-window size where observations are sampled in the sub-sampling procedure (if vartype=SubSamp). For increasing winconst increasing sub-window sizes are obtained. Optional argument, the default is 1. See Details for more information.
winstp	Numeric; a value in $(0, 1]$ for computing the sub-window step (in the sub-sampling procedure). This value denote the proportion of the sub-window size. Optional argument, the default is 0.5. See Details for more information.

Details

Note, that the standard likelihood may be seen as particular case of the composite likelihood. In this respect `FitComposite` provides maximum likelihood fitting, including also the restricted and tapered versions, of Gaussian random fields.

With data, coordx, coordy, coordt, grid and replicates parameters:

- If data is a numeric d -dimensional vector, coordx and coordy are two numeric d -dimensional vectors (or coordx is $(d \times 2)$ -matrix and coordy=NULL), coordt=NULL, grid=FALSE and

replicates=1, then the data are interpreted as a single spatial realisation observed on d spatial sites;

- If data is a numeric $(n \times d)$ -matrix, coordx and coordy are two numeric d -dimensional vectors (or coordx is $(d \times 2)$ -matrix and coordy=NULL), coordt=NULL, grid=FALSE and replicates=n, then the data are interpreted as n iid replications of a spatial random field observed on d spatial sites.
- If data is a numeric $(d \times d)$ -matrix, coordx and coordy are two numeric d -dimensional vectors, coordt=NULL, grid=TRUE and replicates=1, then the data are interpreted as a single spatial random field realisation observed on d equispaced spatial sites (named regular grid).
- If data is a numeric $(d \times d \times n)$ -array, coordx and coordy are two numeric d -dimensional vectors, coordt=NULL, grid=TRUE and replicates=n, then the data are interpreted as n iid realisations of a spatial random field observed on d equispaced spatial sites.
- If data is a numeric $(t \times d)$ -matrix, coordx and coordy are two numeric d -dimensional vectors (or coordx is $(d \times 2)$ -matrix and coordy=NULL), coordt is a numeric t -dimensional vector, grid=FALSE and replicates=1, then the data are interpreted as a single spatial-temporal realisation of a random field observed on d spatial sites and for t times.
- If data is a numeric $(t \times d \times n)$ -array, coordx and coordy are two numeric d -dimensional vectors (or coordx is $(d \times 2)$ -matrix and coordy=NULL), coordt is a numeric t -dimensional vector, grid=FALSE and replicates=n, then the data are interpreted as n iid realisations of a spatial-temporal random field observed on d spatial sites and for t times.
- If data is a numeric $(d \times d \times t)$ -array, coordx and coordy are two numeric d -dimensional vectors, coordt is a numeric t -dimensional vector, grid=TRUE and replicates=1, then the data are interpreted as a single spatial-temporal realisation of a random field observed on d equispaced spatial sites and for t times.
- If data is a numeric $(d \times d \times t \times n)$ -array, coordx and coordy are two numeric d -dimensional vectors, coordt is a numeric t -dimensional vector, grid=TRUE and replicates=n, then the data are interpreted as n iid realisation of a spatial-temporal random field observed on d equispaced spatial sites and for t times.

The `corrmodel` parameter allows to select a specific correlation function for the random field. The implemented spatial correlation models are:

1. cauchy;
2. exponential;
3. gauss (Gaussian);
4. gencauchy (generalised Cauchy);
5. spherical;
6. stable (or powered exponential);
7. wave;
8. whittlematern (Whittle-Matern).

The implemented non-separable spatio-temporal correlation models are:

1. iacocesare (Iaco-Cesare);
2. gneiting (Gneiting);

3. porcu (Porcu).

Separable spatio-temporal correlation models are easily obtained by a product between a spatial and a temporal correlation. The implemented function are:

1. `exp_cauchy` (exponential-Cauchy);
2. `exp_exp` (exponential-exponential);
3. `exp_gauss` (exponential-Gaussian);
4. `matern_cauchy` (Whittle-Matern-Cauchy);
5. `matern_exp` (Whittle-Matern-exponential).

See for more details [CovarianceFct](#).

The `likelihood` parameter represents the composite-likelihood configurations. The settings alternatives are:

1. `Conditional`, the composite-likelihood is formed by conditionals likelihoods;
2. `Marginal`, the composite-likelihood is formed by marginals likelihoods;
3. `Full`, the composite-likelihood turns out to be the standard likelihood;

The `margins` parameter concerns only max-stable fields and indicates how the margins are considered. The options are `Gev` or `Frechet`, where in the former case the marginals are supposed generalized extreme value distributed and in the latter case unit Frechet distributed.

The `maxdist` parameter set the maximum spatial distance below which pairs of sites with inferior distances are considered in the composite-likelihood. This can be inferior of the effective maximum spatial distance. **Note** that this corresponds to use a weighted composite-likelihood with binary weights. Pairs with distance less than `maxdist` have weight 1 and are included in the likelihood computation, instead those with greater distance have weight 0 and then excluded. The default is `NULL`, in this case the effective maximum spatial distance between sites is considered.

The same arguments of `maxdist` are valid for `maxtime` but here the weighed composite-likelihood regards the case of spatial-temporal field. At the moment is implemented only for Gaussian random fields. The default is `NULL`, in this case the effective maximum temporal lag between pairs of observations is considered.

The `model` parameter indicates the type of random field considered, for instance `model=Gaussian` denotes a Gaussian random field. Accordingly, this also determines the analytical expression of the finite dimensional distribution associated with the random field. The available options are:

- `Gaussian`, for a Gaussian random field (see i.e. Wackernagel, H. 1998);
- `BinaryGauss`, for a Binary random field (see Heagerty and Lele 1998)
- `BrowResn`, for a Brown-Resnick max-stable random field (see Kabluchko, Z. et al. 2009);
- `ExtGauss`, for a Extremal Gaussian max-stable random field (see Schlather, M. 2002);
- `ExtT`, for a Extremal t max-stable random field (see Davison, A. C. et al. 2011);

Note, that only for the Gaussian case the estimation procedure is implemented for spatial and spatial-temporal random fields.

The `start` parameter allows to specify starting values. If `start` is omitted the routine is computing the starting values using the weighted moment estimator.

The `taper` parameter, optional in case that `type=Tapering`, indicates the type of taper correlation model. At the moment the implemented models are:

1. Wendland type 1;
2. Wendland type 2;
3. Wendland type 3.

For more details Furrer et al. (2006) and see Kaufman et al. (2008). **ATTENTION!** Insert also a value for the `maxdist` parameter in order to set the upper bound of the compact support; if no `maxdist` is inserted then the effective maximum spatial distance is considered and therefore the tapering approach does not have any effect.

The `threshold` parameter indicates the value (common for all the spatial sites) above which the values of the underlying Gaussian latent process are considered successes events (values below are instead failures). See e.g. Heagerty and Lele (1998) for more details.

The `type` parameter represents the type of likelihood used in the composite-likelihood definition. The possible alternatives are listed in the following scheme.

1. If a Gaussian random field is considered (`model=Gaussian`):
 - If the composite is formed by marginal likelihoods (`likelihood=Marginal`):
 - Pairwise, the composite-likelihood is defined by the pairwise likelihoods;
 - Difference, the composite-likelihood is defined by likelihoods which are obtained as difference of the pairwise likelihoods.
 - If the composite is formed by conditional likelihoods (`likelihood=Conditional`)
 - Pairwise, the composite-likelihood is defined by the pairwise conditional likelihoods.
 - If the composite is formed by a full likelihood (`likelihood=Full`):
 - Standard, the objective function is the classical multivariate likelihood;
 - Restricted, the objective function is the restricted version of the full likelihood (e.g. Harville 1977, see **References**);
 - Tapering, the objective function is the tapered version of the full likelihood (e.g. Kaufman et al. 2008, see **References**). At the moment is implemented only for spatial Gaussian random fields.

The `vartype` parameter specifies the method used to compute the estimates' variances. In particular for estimating the variability matrix J in the Godambe expression matrix. This parameter is considered if `varest=TRUE`. The options are:

- `SubSamp` (the default), indicates the Sub-Sampling method;
- `Theoretical`, denotes that the variability matrix is computed using the exact analytical expression. At the moment is implemented for spatial Gaussian random fields when using difference composite likelihood, namely `Model='Gaussian'` and `likelihood='Difference'`;
- `Sampling`, indicates that the variability matrix is estimated by the sample contro-part (available only for n iid replications of the random field, i.e. `replicates=n`);

The `weighted` parameter specifies if the likelihoods forming the composite-likelihood must be weighted. If `TRUE` the weights are selected by opportune procedures that improve the efficient of the maximum composite-likelihood estimator (not implemented yet). If `FALSE` the efficient improvement procedure is not used.

For computing the standard errors by the sub-sampling procedure, `winconst` and `winstp` parameters represent respectively a positive constant used to determine the sub-window size and the step with which the sub-window moves.

In the spatial case (subset of R^2), the domain is seen as a rectangle $B \times H$, therefore the size of the sub-window side b is given by $b = \text{winconst} \times \sqrt{B}$ (similar is of h). For a complete description see Lee and Lahiri (2002). By default `winconst` is set $B/(2 \times \sqrt{B})$. The `winstp` parameter is used to determine the sub-window step. The latter is given by the proportion of the sub-window size, so that when `winstp=1` there is not overlapping between contiguous sub-windows. In the spatial case by default `winstp=0.5`. The sub-window is moved by successive steps in order to cover the entire spatial domain. Observations, that fall in disjoint or overlapping windows are considered independent samples.

In the spatio-temporal case the subsampling is meant only in time as described by Li et al. (2007). Thus, `winconst` represents the length of the temporal sub-window. By default the size of the sub-window is computed following the rule established in Li et al. (2007). By default `winstp` is the time step.

Observe that in the spatio-temporal case, the returned values by `srange` and `trange`, represent respectively the minimum and maximum of the marginal spatial distances and those of the temporal separations. Thus, the minimum being not the overall (i.e. considering the spatio-temporal coordinates) is not zero, as one could be expect and the latter can be easily added by the user.

Value

Returns an object of class `FitComposite`. An object of class `FitComposite` is a list containing at most the following components:

<code>clic</code>	The composite information criterion, if the full likelihood is considered then it coincides with the Akaike information criterion;
<code>coor dx</code>	A d -dimensional vector of spatial coordinates;
<code>coor dy</code>	A d -dimensional vector of spatial coordinates;
<code>coor dt</code>	A t -dimensional vector of temporal coordinates;
<code>convergence</code>	A string that denotes if convergence is reached;
<code>corrmodel</code>	The correlation model;
<code>data</code>	The vector or matrix or array of data;
<code>fixed</code>	The vector of fixed parameters;
<code>iterations</code>	The number of iteration used by the numerical routine;
<code>likelihood</code>	The configuration of the composite likelihood;
<code>logCompLik</code>	The value of the log composite-likelihood at the maximum;
<code>lonlat</code>	The type of coordinates;
<code>message</code>	Extra message passed from the numerical routines;
<code>model</code>	The density associated to the likelihood objects;
<code>numcoord</code>	The number of spatial coordinates;
<code>numrep</code>	The number of the iid replicatations of the random field;
<code>numtime</code>	The number the temporal realisations of the random field;

param	The vector of parameters' estimates;
srange	The minimum and maximum spatial distance (see Details). The maximum is <code>maxdist</code> , if inserted, rather the effective maximum distance;
stderr	The vector of standard errors;
sensmat	The sensitivity matrix;
varcov	The matrix of the variance-covariance of the estimates;
varimat	The variability matrix;
vartype	The method used to compute the variance of the estimates;
trange	The minimum and maximum temporal separation (see Details). The maximum is <code>maxtime</code> , if inserted, rather than the effective maximum separation;
threshold	The threshold used in the binary random field.
type	The type of the likelihood objects.
winconst	The constant use to compute the window size in the sub-sampling procedure;
winstp	The step used for moving the window in the sub-sampling procedure

Author(s)

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See Also

[CovarianceFct](#), [GaussRF](#), [MaxStableRF](#), [WLeastSquare](#), [optim](#)

Examples

```

library(CompRandFld)
library(RandomFields)
library(spam)
set.seed(3132)

# Define the spatial-coordinates of the points:
x <- runif(100, 0, 10)
y <- runif(100, 0, 10)

#####
###
### Example 1. Maximum likelihood fitting of
### Gaussian random fields with exponential correlation.
### One spatial replication.
### Likelihood setting: composite with
### marginal pairwise likelihood objects.
###
#####

# Set the model's parameters:
corrmodel <- "exponential"
mean <- 0
sill <- 1
nugget <- 0
scale <- 1.5

# Simulation of the spatial Gaussian random field:
data <- RFsim(x, y, corrmodel=corrmodel, param=list(mean=mean,
sill=sill,nugget=nugget,scale=scale))$data

# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(data, x, y, corrmodel=corrmodel, maxdist=5,
varest=TRUE,fixed=list(mean=mean,nugget=nugget))

# Results:
print(fit)

#####
###
### Example 2. Maximum likelihood fitting of
### Gaussian random fields with exponential correlation.
### One spatial replication.
### Likelihood setting: standard full likelihood.
###
#####

# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(data, x, y, corrmodel=corrmodel,likelihood='Full',
type='Standard',varest=TRUE,fixed=list(mean=mean,
nugget=nugget))

```

```

# Results:
print(fit)

#####
###
### Example 3. Maximum likelihood fitting of
### Gaussian random fields with exponential correlation.
### One spatial replication.
### Likelihood setting: tapered full likelihood.
###
#####

# Remove the symbol # in order to run this example.
# Maximum composite-likelihood fitting of the random field:
#fit <- FitComposite(data, x, y, corrmodel=corrmodel,likelihood='Full',
#                    type='Tapering', taper="Wendland1",maxdist=4,
#                    varest=TRUE,fixed=list(mean=mean,nugget=nugget))
#
# Results:
#print(fit)

#####
###
### Example 4. Maximum likelihood fitting of
### Gaussian random field with double-exponential correlation.
### One spatio-temporal replication.
### Likelihood setting: composite with conditional pairwise
### likelihood objects.
###
#####

# Define the temporal sequence:
time <- seq(1, 10, 1)

# Simulation of the spatial-temporal Gaussian random field:
data <- RFsim(x,y,time,corrmodel="exp_exp",param=list(mean=0,
              scale_s=1,scale_t=1,sill=sill,nugget=nugget))$data

# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(data,x,y,time,corrmodel="exp_exp",maxtime=3,
                    maxdist=10,likelihood="Conditional",type="Pairwise",
                    start=list(scale_s=1,scale_t=1,sill=.5),
                    fixed=list(mean=mean,nugget=nugget))

# Results:
print(fit)

#####
###
### Example 5. Maximum composite-likelihood fitting of
### max-stable random fields. Extremal Gaussian model with
### exponential correlation. n iid spatial replications.

```

```

### Likelihood setting: composite with marginal pairwise
### likelihood objects.
###
#####

# Simulation of a max-stable random field in the specified points:
data <- RFsim(x, y, corrmmodel=corrmmodel, model="ExtGauss", replicates=30,
             param=list(mean=mean,sill=sill,nugget=nugget,scale=scale))$data

# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(data, x, y, corrmmodel=corrmmodel, model='ExtGauss',
                  replicates=30, varest=TRUE, vartype='Sampling',
                  margins="Frechet",start=list(sill=sill,scale=scale))

# Results:
print(fit)

#####
###
### Example 6. Maximum likelihood fitting of
### Binary-Gaussian random fields with exponential correlation.
### One spatial replication.
### Likelihood setting: composite with marginal pairwise
### likelihood objects.
###
#####

set.seed(3128)

x <- runif(300, 0, 10)
y <- runif(300, 0, 10)

# Simulation of the spatial Binnry-Gaussian random field:
data <- RFsim(x, y, corrmmodel=corrmmodel, model="BinaryGauss",
             threshold=0, param=list(mean=mean,sill=.8,
             nugget=nugget,scale=scale))$data

# Maximum composite-likelihood fitting of the random field:
fit <- FitComposite(data, x, y, corrmmodel=corrmmodel, threshold=0,
                  model="BinaryGauss", fixed=list(nugget=nugget,
                  mean=0),start=list(scale=.1,sill=.1))

# Results:
print(fit)

```

Description

the function returns the parameters' estimates and the variances of the estimates (if required) of the generalized extreme value distribution for a given dataset of extreme values.

Usage

```
FitGev(data, method='Nelder-Mead', start, varest=FALSE)
```

Arguments

data	A vector of extreme values.
method	The optimization method (see optim for details). 'Nelder-Mead' is the default.
start	A named list with the initial values for the parameters over which the likelihood is to be maximized.
varest	Logical; if TRUE the estimate' variances and the standard errors are returned, instead if FALSE (the default) only the estimate are computed.

Details

If start is omitted the routine is computing the starting values using moment estimators.

Value

The returned object is a list with:

param	The vector of parameters' estimates.
varcov	The matrix of the variance-covariance of the estimates.
stderr	The vector of the standard errors.

Author(s)

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References

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See Also

[GevLogLik](#), [optim](#)

GevLogLik

Log-Likelihood of the GEV Distribution

Description

The function returns the log-likelihood value of the Generalized Extreme Value Distribution for a given set of data and parameters.

Usage

```
GevLogLik(data, numdata, param)
```

Arguments

data	A vector of extreme values.
numdata	The number of data observations.
param	The vector of GEV parameters (location, scale and shape).

Value

The log-likelihood value is returned.

Author(s)

Simone Padoan, <simone.padoan@stat.unipd.it>, <http://homes.stat.unipd.it/padoan>.

References

de Haan, L. and Ferreira, A. (2006) *Extreme Value Theory An Introduction*. Springer Verlag, New York.

HypoTest

Statistical Hypothesis Tests for Nested Models

Description

The function performs statistical hypothesis tests for nested models based on composite likelihood versions of: Wald-type, score-type and Wilks-type (likelihood ratio) statistics.

Usage

```
HypoTest(object1, object2, ..., statistic)
```

Arguments

object1	An object of class <code>FitComposite</code> .
object2	An object of class <code>FitComposite</code> that is a nested model within object1.
...	Further successively nested objects.
statistic	String; the name of the statistic used within the hypothesis test (see Details).

Details

The implemented hypothesis tests for nested models are based on the following statistics:

1. Wald-type (Wald);
2. Score-type, also known as Rao-type (Rao);
3. Wilks-type; also known as the composite likelihood ratio statistic. Available are variants of the basic version, in particular:
 - Rotnitzky and Jewell adjustment (WilksRJ);
 - Satterhwaite adjustment (WilksS);
 - Chandler and Bate adjustment (WilksCB);
 - Pace, Salvan and Sartori adjustment (WilksPSS);

More specifically, consider an p -dimensional random vector \mathbf{Y} with probability density function $f(\mathbf{y}; \theta)$, where $\theta \in \Theta$ is a q -dimensional vector of parameters. Suppose that $\theta = (\psi, \tau)$ can be partitioned in a q' -dimensional subvector ψ and q'' -dimensional subvector τ . Assume also to be interested in testing the specific values of the vector ψ . Then, one can use some statistical hypothesis tests for testing the null hypothesis $H_0 : \psi = \psi_0$ against the alternative $H_1 : \psi \neq \psi_0$. Composite likelihood versions of 'Wald' and 'score' statistics have the usual asymptotic chi-square distribution with q' degree of freedom. The Wald-type statistic is

$$W = (\hat{\psi} - \psi_0)^T (G^{\psi\psi})^{-1} (\hat{\theta}) (\hat{\psi} - \psi_0),$$

where $G_{\psi\psi}$ is the $q' \times q'$ submatrix of the Godambe information pertaining to ψ and $\hat{\theta}$ is the maximum likelihood estimator from the full model. The score-type statistic (Rao-type) is

$$W = s_{\psi}\{\psi_0, \hat{\tau}(\psi_0)\}^T H^{\psi\psi}(\hat{\theta}_{\psi}) \{G^{\psi\psi}(\hat{\theta}_{\psi})\}^{-1} H^{\psi\psi}(\hat{\theta}_{\psi}) s_{\psi}\{\psi_0, \hat{\tau}(\psi_0)\},$$

where $H^{\psi\psi}$ is the $q' \times q'$ submatrix of the inverse of $H(\theta)$ pertaining to ψ (the same for G) and $\hat{\theta}_{\psi}$ is the constrained maximum likelihood estimate of θ for fixed ψ . These two statistics can be called from the routine `HypoTest` assigning at the argument `statistic` respectively the values: `Wald` and `Rao`.

Alternatively to the Wald-type and score-type statistics one can use the composite version of the Wilks-type or likelihood ratio statistic, given by

$$W = 2[Cl(\hat{\theta}; \mathbf{y}) - Cl\{\psi_0, \hat{\tau}(\psi_0); \mathbf{y}\}].$$

The asymptotic distribution of the composite likelihood ratio statistic is given by

$$W \sim \sum_i \lambda_i \chi^2,$$

for $i = 1, \dots, q'$, where χ_i^2 are q' iid copies of a chi-square one random variable and $\lambda_1, \dots, \lambda_{q'}$ are the eigenvalues of the matrix $(H^{\psi\psi})^{-1}G^{\psi\psi}$. There exist several adjustments to the composite likelihood ratio statistic in order to get an approximated $\chi_{q'}^2$. For example, Rotnitzky and Jewell (1990) proposed the adjustment $W' = W/\bar{\lambda}$ where $\bar{\lambda}$ is the average of the eigenvalues λ_i . This statistic can be called within the routine by the value: `WilksRJ`. A better solution is proposed by Satterthwaite (1946) defining $W'' = \nu W/(q'\bar{\lambda})$, where $\nu = (\sum_i \lambda)^2 / \sum_i \lambda_i^2$ for $i = 1 \dots, q'$, is the effective number of the degree of freedom. Note that in this case the distribution of the likelihood ratio statistic is a chi-square random variable with ν degree of freedom. This statistic can be called from the routine assigning the value: `WilksS`. For the adjustments suggested by Chandler and Bate (2007) and Pace, Salvan and Sartori (2011) we refer to the articles (see **References**), these versions can be called from the routine assigning respectively the values: `WilksCB` and `WilksPSS`.

Value

An object of class `c("data.frame")`. The object contain a table with the results of the tested models. The rows represent the responses for each model and the columns the following results:

<code>Num.Par</code>	The number of the model's parameters.
<code>Diff.Par</code>	The difference between the number of parameters of the model in the previous row and those in the actual row.
<code>Df</code>	The effective number of degree of freedom of the chi-square distribution.
<code>Chisq</code>	The observed value of the statistic.
<code>Pr(>chisq)</code>	The p-value of the quantile <code>Chisq</code> computed using a chi-squared distribution with <code>Df</code> degrees of freedom.

Author(s)

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References

- Chandler, R. E., and Bate, S. (2007). Inference for Clustered Data Using the Independence log-likelihood. *Biometrika*, **94**, 167–183.
- Pace, L., Salvan, A. and Sartori, N. (2011). Adjusting Composite Likelihood Ratio Statistics. *Statistica Sinica*, **21**, 129–148.
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See Also

[FitComposite](#).

Examples

```

library(CompRandFld)
library(RandomFields)
set.seed(3451)

# Define the spatial-coordinates of the points:
x <- runif(300, 0, 10)
y <- runif(300, 0, 10)

#####
###
### Example 1. Composite likelihood-based hypothesis testing.
### Simulation of a Gaussian spatial random field with
### stable correlation.
### Estimation by composite likelihood using the setting:
### marginal pairwise likelihood objects.
###
#####

# Set the model's parameters:
corrmodel <- "stable"
mean <- 0
sill <- 1
nugget <- 1
scale <- 1
power <- 1.3

# Simulation of the spatial Gaussian random field:
data <- RFsim(x, y, corrmodel=corrmodel, param=list(mean=mean,
            sill=sill,nugget=nugget,scale=scale,power=power))$data

# Maximum composite-likelihood fitting of the random field, full model:
fit1 <- FitComposite(data, x, y, corrmodel=corrmodel, maxdist=5,
            varest=TRUE,fixed=list(nugget=1))

# Maximum composite-likelihood fitting of the random field, first nested model:
fit2 <- FitComposite(data, x, y, corrmodel=corrmodel, maxdist=5,
            varest=TRUE,fixed=list(nugget=1,sill=1))

# Maximum composite-likelihood fitting of the random field, second nested model:
fit3 <- FitComposite(data, x, y, corrmodel=corrmodel, maxdist=5,
            varest=TRUE,fixed=list(nugget=1,sill=1,mean=0,power=1.3))

# Hypothesis testing results:
# composite Wald-type statistic:
HypoTest(fit1, fit2, fit3, statistic='Wald')

# composite score-type statistic:
HypoTest(fit1, fit2, fit3, statistic='Rao')

# composite likelihood ratio statistic with RJ adjustment:
HypoTest(fit1, fit2, fit3, statistic='WilksRJ')

```

```
# composite likelihood ratio statistic with S adjustment:
HypoTest(fit1, fit2, fit3, statistic='WilksS')

# composite likelihood ratio statistic with CB adjustment:
HypoTest(fit1, fit2, fit3, statistic='WilksCB')

# composite likelihood ratio statistic with PSS adjustment:
HypoTest(fit1, fit2, fit3, statistic='WilksPSS')
```

InitParam

Initializes the Parameters for Estimation Procedures

Description

Subroutine called by the fitting procedures. The procedure initializes the parameters for the fitting procedure.

Usage

```
InitParam(coordx, coordy, coordt, corrmodel, data, fcall, fixed, grid,
          likelihood, lonlat, margins, maxdist, maxtime, model, numblock,
          param, parscale, paramrange, replicates, start, threshold,
          type, typereal, varest, vartype, weighted, winconst, winstp)
```

Arguments

coordx	A numeric ($d \times 2$)-matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
coordt	A numeric vector assigning 1-dimension of temporal coordinates.
corrmodel	String; the name of a correlation model.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
fcall	String; "fitting" to call the fitting procedure and "simulation" to call the simulation procedure.
fixed	A named list giving the values of the parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the composite likelihood.
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
margins	String; the type of the marginal distribution of the max-stable field.

maxdist	Numeric; an optional positive value indicating the maximum spatial distance considered in the composite-likelihood computation.
maxtime	Numeric; an optional positive value indicating the maximum temporal lag considered in the composite-likelihood computation.
model	String; the density associated to the likelihood objects. Gaussian is the default.
numblock	Numeric; the observation size of the underlying random field. Only in case of max-stable random fields and in the simulation.
param	A numeric vector of parameter values required in the simulation procedure of random fields.
parscale	A numeric vector of scaling factor to improve the maximizing procedure, see optim .
paramrange	A numeric vector of parameters ranges, see optim .
replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.
start	A named list with the initial values of the parameters that are used by the numerical routines in maximization procedure.
threshold	Numeric; a value indicating a threshold for the binary random field.
type	String; the type of likelihood objects. Temporary value set to be "WLeast-Square" (weighed least-square) in order to compute the starting values.
typereal	String; the real type of likelihood objects. See FitComposite .
varest	Logical; if TRUE the estimates' variances and standard errors are returned. FALSE is the default.
vartype	String; the type of estimation method for computing the estimate variances, see the Section Details .
weighted	Logical; if TRUE the likelihood objects are weighted, see FitComposite .
winconst	Numeric; a positive real value indicating the sub-window in the sub-sampling procedure. See FitComposite .
winstp	Numeric; a value in $(0, 1]$ for defining the window step. See FitComposite .

Author(s)

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See Also

[FitComposite](#)

Likelihood

*Optimizes the Log Likelihood***Description**

Subroutine called by FitComposite. The procedure estimates the model parameters by maximization of the log-likelihood.

Usage

```
Likelihood(corrmodel, data, fixed, flagcor, flagnuis, grid, lower,
           model, namescorr, namesnuis, namesparam, numcoord, numpairs,
           numparamcor, numrep, numtime, optimizer, param, setup,
           spacetime, varest, taper, type, upper)
```

Arguments

corrmodel	Numeric; the id of the correlation model.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
flagcor	A numeric vector of flags denoting which correlation parameters have to be estimated.
flagnuis	A numeric vector of flags denoting which nuisance parameters have to be estimated.
fixed	A numeric vector of parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
lower	A numeric vector with the lower bounds of the parameters' ranges.
model	Numeric; the id value of the density associated to the likelihood objects.
namescorr	String; the names of the correlation parameters.
namesnuis	String; the names of the nuisance parameters.
namesparam	String; the names of the parameters to be maximised.
numcoord	Numeric; the number of coordinates.
numpairs	Numeric; the number of pairs.
numparamcor	Numeric; the number of the correlation parameters.
numrep	Numeric; the number of iid replications.
numtime	Numeric; the number of temporal observations.
optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.
param	A numeric vector of parameters.
setup	A List of useful components for the estimation based on the maximum tapered likelihood.

spacetime	Logical; if the random field is spatial (FALSE) or spatio-temporal (TRUE).
varest	Logical; if TRUE the estimate' variances and standard errors are returned. FALSE is the default.
taper	String; the name of the taper correlation function.
type	String; the type of the likelihood objects. If Pairwise (the default) then the marginal composite likelihood is formed by pairwise marginal likelihoods.
upper	A numeric vector with the upper bounds of the parameters' ranges.

Author(s)

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See Also

[FitComposite](#)

MomEst

Estimation of the GEV parameters by the Method of Moments

Description

Using the moment estimator, the function returns the parameter estimates of the generalized extreme value distribution for a given dataset of extreme values.

Usage

```
MomEst(data, n)
```

Arguments

data	A vector of extreme values.
n	The number of observations.

Value

The returned object is a list with:

location	The location estimate.
scale	The scale estimate.
shape	The shape estimate.

Author(s)

Simone Padoan, <simone.padoan@stat.unipd.it>, <http://homes.stat.unipd.it/padoan>.

References

de Haan, L. and Ferreira, A. (2006) *Extreme Value Theory An Introduction*. Springer Verlag, New York.

See Also

[GevLogLik](#), [FitGev](#)

NuisanceParam *Lists the Nuisance Parameters of a Random Field*

Description

Subroutine called by InitParam and other procedures. The procedure returns a list with the nuisance parameters of a given random field model.

Usage

```
NuisanceParam(model)
```

Arguments

model String; the name of a random field.

Author(s)

Simone Padoan, <simone.padoan@stat.unipd.it>, <http://homes.stat.unipd.it/padoan>.

See Also

[FitComposite](#)

RFsim *Simulation of Gaussian, Binary and Max-stable Random Fields*

Description

Simulation of spatial and spatio-temporal Gaussian, binary and max-stable random fields. The function returns one or more replications of a random field for a given covariance model and covariance parameters.

Usage

```
RFsim(coordx, coordy=NULL, coordt=NULL, corrmodel, grid=FALSE,  
      model='Gaussian', numblock=NULL, param, replicates=1,  
      threshold=NULL)
```

Arguments

coordx	A numeric ($d \times 2$)-matrix (where d is the number of spatial sites) assigning 2-dimensions of spatial coordinates or a numeric d -dimensional vector assigning 1-dimension of spatial coordinates.
coordy	A numeric vector assigning 1-dimension of spatial coordinates; coordy is interpreted only if coordx is a numeric vector or grid=TRUE otherwise it will be ignored. Optional argument, the default is NULL then coordx is expected to be numeric a ($d \times 2$)-matrix.
coor dt	A numeric vector assigning 1-dimension of temporal coordinates. At the moment implemented only for the Gaussian case. Optional argument, the default is NULL then a spatial random field is expected.
corrmodel	String; the name of a correlation model, for the description see the Section Details .
grid	Logical; if FALSE (the default) the data are interpreted as spatial or spatial-temporal realisations on a set of non-equispaced spatial sites (irregular grid).
model	String; the type of random field and therefore the densities associated to the likelihood objects. Gaussian is the default, see the Section Details .
numblock	Numeric; the observation size of the underlying random field. Only in case of max-stable random fields.
param	A list of parameter values required in the simulation procedure of random fields, see Examples .
replicates	Numeric; a positive integer denoting the number of independent and identically distributed (iid) replications of a spatial or spatial-temporal random field. Optional argument, the default value is 1 then a single realisation is considered.
threshold	Numeric; a value indicating a threshold for the binary random field. Optional in the case that model is BinaryGauss, see the Section Details .

Details

Note that this function is also interfaced to the **R** package **RandomFields**, using fast routines therein developed for the simulation of random fields, see for example [GaussRF](#), [MaxStableRF](#), ect.

Value

Returns an object of class `RFsim`. An object of class `RFsim` is a list containing at most the following components:

coordx	A d -dimensional vector of spatial coordinates;
coordy	A d -dimensional vector of spatial coordinates;
coor dt	A t -dimensional vector of temporal coordinates;
corrmodel	The correlation model;
data	The vector or matrix or array of data, see FitComposite ;
model	The type of random field, see FitComposite .
numcoord	The number of spatial coordinates;

numtime	The number the temporal realisations of the random field;
param	The vector of parameters' estimates;
randseed	The seed used for the random simulation;
replicates	The number of the iid replicatations of the random field;
spacetime	TRUE if spatio-temporal and FALSE if spatial random field;
threshold	The threshold for deriving the binary random field.

Author(s)

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See Also

[CovarianceFct](#), [GaussRF](#), [MaxStableRF](#)

Examples

```
library(CompRandFld)
library(RandomFields)

#####
###
### Example 1. Simulation of a Gaussian random field.
### Gaussian random fields with Whittle-Matern correlation.
### One spatial replication.
###
###
#####

# Define the spatial-coordinates of the points:
x <- runif(500, 0, 2)
y <- runif(500, 0, 2)

set.seed(261)
# Simulation of a spatial Gaussian random field:
sim <- RFsim(x, y, corrmmodel="matern", param=list(smooth=0.5,
          mean=0,sill=1,scale=0.2,nugget=0))

#####
###
### Example 2. Simulation of a binary random field based on
### the latent Gaussian random field with exponential correlation.
### One spatial replication on a regular grid
###
###
#####

# Define the spatial-coordinates of the points:
x <- seq(0, 1, 0.02)
```

```

y <- seq(0, 1, 0.02)

set.seed(251)

# Simulation of a spatial binary random field:
sim <- RFsim(x, y, corrmmodel="exponential", grid=TRUE,
            model="BinaryGauss", threshold=0,
            param=list(nugget=0,mean=0,scale=.1,sill=1))

image(x,y,sim$data)

#####
###
### Example 3. Simulation of a max-stable random
### extremal-t type with exponential correlation.
### One spatial replication on a regular grid
###
###
#####

set.seed(341)

# Simulation of a spatial binary random field:
sim <- RFsim(x, y, corrmmodel="exponential", grid=TRUE, model="ExtT",
            numblock=500, param=list(nugget=0,mean=0,scale=.1,
            sill=1,df=8))

image(x,y,log(sim$data))

#####
###
### Example 4. Simulation of a Gaussian random field.
### with double exponential correlation.
### One spatio-temporal replication.
###
###
#####

# Define the spatial-coordinates of the points:
x <- seq(0, 1, 0.05)
y <- seq(0, 1, 0.05)
# Define the temporal-coordinates:
times <- seq(1, 10, 1)

# Simulation of a spatial Gaussian random field:
sim <- RFsim(x, y, times, corrmmodel="exp_exp", grid=TRUE,
            param=list(nugget=0,mean=0,scale_s=0.3,
            scale_t=0.5,sill=1))

# For a simple animation movie
# library(animation)
# saveMovie(for (i in 1:length(times)) image(x,y,sim$data[,i]),

```

```
# height=300,width=500,interval=1,
# outdir = "c:/",movie.name = "spacetime_animation.mpg")
```

WLeastSquare

WLS of Gaussian and Max-Stable Random Fields

Description

the function returns the parameters' estimates and the estimates' variances of a random field obtained by the weighed least squares estimator.

Usage

```
WLeastSquare(data, coordx, coordy=NULL, coordt=NULL, corrmodel,
             fixed=NULL, grid=FALSE, lonlat=FALSE, maxdist=NULL,
             maxtime=NULL, model='Gaussian', optimizer='Nelder-Mead',
             numbins=NULL, replicates=1, start=NULL, weighted=FALSE)
```

Arguments

data	A d -dimensional vector (a single spatial realisation) or a $(n \times d)$ -matrix (n iid spatial realisations) or a $(d \times d)$ -matrix (a single spatial realisation on regular grid) or an $(d \times d \times n)$ -array (n iid spatial realisations on regular grid) or a $(t \times d)$ -matrix (a single spatial-temporal realisation) or an $(t \times d \times n)$ -array (n iid spatial-temporal realisations) or or an $(d \times d \times t \times n)$ -array (a single spatial-temporal realisation on regular grid) or an $(d \times d \times t \times n)$ -array (n iid spatial-temporal realisations on regular grid). See FitComposite for details.
coordx	A numeric $(d \times 2)$ -matrix (where d is the number of spatial sites) assigning 2-dimensions of spatial coordinates or a numeric d -dimensional vector assigning 1-dimension of spatial coordinates.
coordy	A numeric vector assigning 1-dimension of spatial coordinates; coordy is interpreted only if coordx is a numeric vector or grid=TRUE otherwise it will be ignored. Optional argument, the default is NULL then coordx is expected to be numeric a $(d \times 2)$ -matrix.
coordt	A numeric vector assigning 1-dimension of temporal coordinates. Optional argument, the default is NULL then a spatial random field is expected.
corrmodel	String; the name of a correlation model, for the description (see FitComposite).
fixed	A named list giving the values of the parameters that will be considered as known values. The listed parameters for a given correlation function will be not estimated, i.e. if <code>list(nugget=0)</code> the nugget effect is ignored.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
maxdist	A numeric value denoting the maximum distance, see Details and FitComposite .

maxtime	Numeric; an optional positive value indicating the maximum temporal lag considered in the composite-likelihood computation (see FitComposite).
model	String; the type of random field. Gaussian is the default, see FitComposite for the different types.
optimizer	String; the optimization algorithm (see optim for details). 'Nelder-Mead' is the default.
numbins	A numeric value denoting the numbers of bins, see the Section Details
replicates	Numeric; a positive integer denoting the number of independent and identically distributed (iid) replications of a spatial or spatial-temporal random field. Optional argument, the default value is 1 then a single realisation is considered.
start	A named list with the initial values of the parameters that are used by the numerical routines in maximization procedure. NULL is the default (see FitComposite).
weighted	Logical; if TRUE then the weighted least square estimator is considered. If FALSE (the default) then the classic least square is used.

Details

The numbins parameter indicates the number of adjacent intervals to consider in order to grouped distances with which to compute the (weighted) lest squares.

The maxdist parameter indicates the maximum distance below which the shorter distances will be considered in the calculation of the (weigthed) least squares.

Value

Returns an object of class WLS. An object of class WLS is a list containing at most the following components:

bins	Adjacent intervals of grouped distances;
bint	Adjacent intervals of grouped temporal separations
centers	The centers of the bins;
coordx	The vector or matrix of spatial coordinates;
coordy	The vector of spatial coordinates;
coordt	The vector of temporal coordinates;
convergence	A string that denotes if convergence is reached;
corrmodel	The correlation model;
data	The vector or matrix of data;
fixed	The vector of fixed parameters;
iterations	The number of iteration used by the numerical routine;
message	Extra message passed from the numerical routines;
model	The type of random fields;
numcoord	The number of spatial coordinates;
numrep	The number of the iid replicatations of the random field;

numtime	The number the temporal realisations of the random field;
param	The vector of parameters' estimates;
srange	The minimum and maximum spatial distance;
trange	The minimum and maximum temporal separations;
variograms	The empirical spatial variogram;
variogramt	The empirical temporal variogram;
variogramst	The empirical spatial-temporal variogram;
weighted	A logical value indicating if its the weighted method;
wls	The value of the least squares at the minimum.

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See Also

[FitComposite](#), [optim](#)

Examples

```
library(RandomFields)
set.seed(2111)

# Set the coordinates of the sites:
x <- runif(100, 0, 10)
y <- runif(100, 0, 10)

#####
###
### Example 1. Least square fitting of a Gaussian random field
### with exponential correlation.
### One spatial replication is simulated.
### Unweighted version (all weights equals to 1).
###
#####
```

```

# Set the model's parameters:
corrmodel <- "exponential"
mean <- 0
sill <- 1
nugget <- 0
scale <- 3

# Simulation of the Gaussian random field:
data <- RFSim(x, y, corrmodel=corrmodel, param=list(mean=mean,
          sill=sill, nugget=nugget, scale=scale))$data

# Least square fitting of the random field:
fit <- WLeastSquare(data, x, y, corrmodel=corrmodel)

# Results:
print(fit)

#####
###
### Example 2. Least square fitting of a max-stable random field
### (Extremal Gaussian model) with exponential correlation
### n iid spatial replications.
### Unweighted version (all weights equals to 1).
###
#####

# Simulation of the max-stable random field:
data <- RFSim(x, y, corrmodel=corrmodel, model="ExtGauss",
          param=list(mean=mean, sill=sill, nugget=nugget,
          scale=scale), replicates=40)$data

# Least square fitting of the random field:
fit <- WLeastSquare(data, x, y, corrmodel=corrmodel, model="ExtGauss",
          replicates=40)

# Results:
print(fit)

#####
###
### Example 3. Least square fitting of a spatio-temporal
### Gaussian random field with double exponential correlation.
### One replication is simulated.
### Weighted version (all weights equals to 1).
###
#####

# Define the temporal sequence:
time <- seq(1, 30, 1)

# Simulation of the Gaussian random field:

```

```

data <- RFsim(x, y, time, corrmodel="exp_exp", param=list(mean=mean,
  scale_s=scale, scale_t=1, sill=sill, nugget=nugget))$data

# Weighted least square estimation:
fit <- WLeastSquare(data, x, y, time, corrmodel="exp_exp", maxdist=5,
  maxtime=5, fixed=list(nugget=nugget),
  start=list(scale_s=0.1, scale_t=0.1, sill=1))

# Results
print(fit)

```

WlsInit

Computes Starting Values based on Weighted Least Squares

Description

Subroutine called by FitComposite. The function returns opportune starting values for the composite-likelihood fitting procedure based on weighed least squares.

Usage

```

WlsInit(coordx, coordy, coordt, corrmodel, data, fcall, fixed, grid,
  likelihood, lonlat, margins, maxdist, maxtime, model, numblock,
  param, parscale, paramrange, replicates, start, threshold,
  type, varest, vartype, weighted, winconst, winstp)

```

Arguments

coordx	A numeric ($d \times 2$)-matrix (where d is the number of points) assigning 2-dimensions of coordinates or a numeric vector assigning 1-dimension of coordinates.
coordy	A numeric vector assigning 1-dimension of coordinates; coordy is interpreted only if coordx is a numeric vector otherwise it will be ignored.
coordt	A numeric vector assigning 1-dimension of temporal coordinates.
corrmodel	String; the name of a correlation model, for the description.
data	A numeric vector or a $(n \times d)$ -matrix or $(d \times d \times n)$ -matrix of observations.
fcall	String; "fitting" to call the fitting procedure and "simulation" to call the simulation procedure.
fixed	A named list giving the values of the parameters that will be considered as known values.
grid	Logical; if FALSE (the default) the data are interpreted as a vector or a $(n \times d)$ -matrix, instead if TRUE then $(d \times d \times n)$ -matrix is considered.
likelihood	String; the configuration of the composite likelihood.
lonlat	Logical; if FALSE (the default), coordx and coordy are interpreted as Cartesian coordinates otherwise they are considered as longitude and latitude.
margins	String; the type of the marginal distribution of the max-stable field.

maxdist	Numeric; an optional positive value indicating the maximum spatial distance considered in the composite-likelihood computation.
maxtime	Numeric; an optional positive value indicating the maximum temporal separation considered in the composite-likelihood computation.
model	String; the name of the model. Here the default is NULL.
numblock	Numeric; the observation size of the underlying random field. Only in case of max-stable random fields and in the simulation.
param	A numeric vector of parameter values required in the simulation procedure of random fields.
parscale	A numeric vector with scaling values for improving the maximisation routine.
paramrange	A numeric vector with the range of the parameter space.
replicates	Logical; if FALSE (the default) one spatial random field is considered, instead if TRUE the data are considered as iid replicates of a field.
start	A numeric vector with starting values.
threshold	Numeric; a value indicating a threshold for the binary random field.
type	String; the type of estimation method.
varest	Logical; if TRUE the estimates' variances and standard errors are returned. FALSE is the default.
vartype	String; the type of estimation method for computing the estimate variances, see the Section Details .
weighted	Logical; if TRUE the likelihood objects are weighted, see FitComposite .
winconst	Numeric; a positive real value indicating the window size used from the sub-sampling method for the estimation of the parameters' variances..
winstp	Numeric; a value in $(0, 1]$ for defining the window step. See FitComposite .

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See Also

[FitComposite](#), [WLeastSquare](#).

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